

Lecture 14: Collisions / Transport

# Collisions

- Coulomb interaction between electrons and ions leads to the scattering of particles -> Collisions
- Interaction occurs only within the Debye sphere
- The angle of deflection depends on how close the particles are approaching each other.



Collisions between the ions

## Small / Large angle scattering

- Deflection depends on how close the particles approach each other
- For a given time a particle moving through the plasma will collide with all particles in a cylinder
- For large angle scattering collisions the distance must be small and so is the radius of the cylinder
- For small angle scattering collisions the radius is much larger
- It turns out that small angle scattering collisions dominate



Distance the particles need to approach for a small angle scattering collision



#### Many body problem

- The plasma has some 10<sup>22</sup> particles. No description is possible that allows for the determination of position and velocity of all these particles
- Only averaged quantities can be described.
- The evolution of the averaged velocity is however influenced by a microscopic process : the collisions
- Each collision can have a different outcome depending on the unknown initial conditions



Depending on the (unknown) initial conditions the outcome of a collision can be very different

# Diffusion of the velocity direction



Initially particles move in one direction

After some time the collisions lead to a random direction

## Diffusion of the velocity

Diffusion coefficient

$$D = \frac{\langle \Delta \theta \Delta \theta \rangle}{2\tau}$$

 Define a function that determines the number of particles moving in a direction given by the angle θ

 $\mathrm{d}N = f(\theta)\mathrm{d}\theta$ 

 Collisions lead to a diffusion in the angle described by

$$\frac{\partial f}{\partial t} = D \frac{\partial^2 f}{\partial \theta^2}$$



Initial distribution of particles moving mostly in the same direction (same angle) are scattered by collisions which randomize the angle of propagation

# Transport in a homogeneous magnetic field

Particles undergo scattering.
 The diffusion coefficient

$$D = \frac{(\Delta x)^2}{2\tau}$$

 Typical step size is the Larmor radius, typical time the collision frequency

$$\Delta x = \rho \qquad \frac{1}{\tau} = \nu$$
$$D = \frac{1}{2}\rho^2 \nu$$



Collisional scattering leads to a random walk of the particle in space

# Transport in a homogeneous magnetic field

Typical values for a reactor

$$D = \frac{1}{2}\rho^{2}\nu \qquad \rho = 4 \,\mathrm{mm} \qquad \nu = 1000 \,\mathrm{s}^{-1}$$
$$D \approx 8 \cdot 10^{-3} \,\mathrm{m}^{2}/\mathrm{s}$$

The particles satisfy a diffusion equation

$$\frac{\partial n}{\partial t} = D \frac{\partial^2 n}{\partial x^2}$$
Rough estimate for  
 $r = a$  gives  
confinement time T
$$\frac{n}{T} = D \frac{n}{a^2}$$

$$a = \sqrt{DT}$$
For T = 3 s
$$a = 15 \text{ cm}$$